

Do It Yourself!

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1. Run HMFA first, to have a feeling of how it works

Please, note that in this example, the structure on the variables doesn't make any sense.

```
library(SensoMineR)
```

```
## Le chargement a nécessité le package : FactoMineR
```

```
?HMFA  
data(wine)  
dim(wine)
```

```
## [1] 21 31
```

```
hierar <- list(c(2,5,3,10,9,2), c(4,2))  
hierar
```

```
## [[1]]  
## [1] 2 5 3 10 9 2  
##  
## [[2]]  
## [1] 4 2
```

```
res.hmfa <- HMFA(wine, H = hierar, type=c("n",rep("s",5)),graph=FALSE)  
names(res.hmfa)
```

```
## [1] "eig"          "group"         "ind"           "partial"       "quanti.var"  
## [6] "quali.var"    "call"
```

```
res.hmfa$eig
```

```
##          eigenvalue percentage of variance cumulative percentage of variance  
## comp 1  1.850020562          41.85452103          41.85452  
## comp 2  0.850890396          19.25038601          61.10491  
## comp 3  0.407053504           9.20910274          70.31401  
## comp 4  0.327584774           7.41121698          77.72523  
## comp 5  0.211693454           4.78931333          82.51454  
## comp 6  0.184243479           4.16829019          86.68283  
## comp 7  0.151762324           3.43344259          90.11627  
## comp 8  0.092312127           2.08845238          92.20473
```

```
## comp 9 0.085169030 1.92684829 94.13157
## comp 10 0.070400479 1.59272733 95.72430
## comp 11 0.049700818 1.12442206 96.84872
## comp 12 0.038018106 0.86011455 97.70884
## comp 13 0.028136547 0.63655600 98.34539
## comp 14 0.021966790 0.49697257 98.84237
## comp 15 0.018103389 0.40956771 99.25193
## comp 16 0.010366410 0.23452773 99.48646
## comp 17 0.008498444 0.19226722 99.67873
## comp 18 0.005681544 0.12853820 99.80727
## comp 19 0.004329531 0.09795050 99.90522
## comp 20 0.004189505 0.09478257 100.00000
```

```
res.hmfa$ind$coord
```

```
##          Dim.1      Dim.2      Dim.3      Dim.4      Dim.5
## 2EL  0.115589635 -0.3839978 -0.63247146 -0.89712973 0.196409100
## 1CHA -1.073384013 -0.8748015 -0.71491035 -1.06137438 0.119528809
## 1FON -0.514932834 -0.8435529 -0.80089351 0.43090044 -0.158675600
## 1VAU -3.312082471 0.1086326 1.12896933 0.19090306 0.426946486
## 1DAM 1.815930443 0.2803452 0.16248808 0.19651032 0.006922444
## 2BOU 0.900713023 -0.3683414 -0.29699797 0.73410583 -0.144255380
## 1BOI 1.210405669 -0.2746202 -0.09748263 0.98165504 0.011017133
## 3EL 0.007179299 0.3242391 -0.85108356 -0.89775551 0.490101883
## DOM1 -0.072338901 -0.4220109 0.30194184 -0.03644779 0.796175745
## 1TUR -0.801117197 -0.0893716 0.69905376 -0.50327664 -0.902505845
## 4EL 0.574079195 0.3282879 0.65002992 -0.37930835 -0.736464625
## PER1 0.666829046 0.5689914 0.55925116 -0.50415500 -0.658246992
## 2DAM 1.608893769 -0.2569175 0.03101310 -0.37739160 -0.103462228
## 1POY 1.516979460 -0.1533753 -0.16734776 -0.20632349 -0.190260417
## 1ING 0.746530209 -0.4027172 -0.63274012 0.30378792 0.175696283
## 1BEN 0.650360906 -0.7940512 -0.04433944 0.86124867 -0.290717306
## 2BEA 0.909112855 -0.3959351 0.93416390 0.26700017 0.970153829
## 1ROC -0.193470297 -0.3921543 1.19642392 -0.26464525 0.246037835
## 2ING -3.441970035 -1.0447129 -0.62878261 0.57610991 -0.433744213
## T1 -0.731136637 2.5119064 -0.16403392 0.46926827 -0.166978738
## T2 -0.582171124 2.5741573 -0.63225169 0.11631811 0.346321799
```

2. Perform your MFAs, at the finest grain, i.e. at the first level of the hierarchy

First, run the separate analyses.

```
res.g1 <- MCA(wine[,1:2],graph = F)
res.g2 <- PCA(wine[,3:7],graph = F)
res.g3 <- PCA(wine[,8:10],graph = F)
res.g4 <- PCA(wine[,11:20],graph = F)
```

Then, get the dimensionality of the data sets.

```
dim(res.g1$eig)
```

```
## [1] 5 3
```

```
dim(res.g2$eig)
```

```
## [1] 5 3
```

```
dim(res.g3$eig)
```

```
## [1] 3 3
```

```
dim(res.g4$eig)
```

```
## [1] 10 3
```

Save the results with the proper number of dimensions.

```
res.g1 <- MCA(wine[,1:2],graph = F)
res.g2 <- PCA(wine[,3:7],graph = F)
res.g3 <- PCA(wine[,8:10],graph = F)
res.g4 <- PCA(wine[,11:20],graph = F,ncp=10)
```

Build a vector of weights (first level of the hierarchy, first node)

```
w.L1.1 <- c(1/rep(res.g1$eig[1,1],5),1/rep(res.g2$eig[1,1],5),
           1/rep(res.g3$eig[1,1],3),1/rep(res.g4$eig[1,1],10))
```

From the original 4 blocks of data to the 4 blocks of coordinates...

```
L1.1 <- cbind(res.g1$ind$coord,res.g2$ind$coord,res.g3$ind$coord,res.g4$ind$coord)
```

Run your first MFA with a PCA program.

```
res.pca.w.L1.1 <- PCA(L1.1,scale.unit = F,col.w = w.L1.1,graph = F,ncp = 20)
res.pca.w.L1.1$ind$coord[,1:5]
```

```
##          Dim.1      Dim.2      Dim.3      Dim.4      Dim.5
## 2EL    0.3297217 -0.3578156 -0.47475980 -1.772718606  0.20494894
## 1CHA  -1.9921118 -0.5669002 -0.67531935 -2.132658250 -0.18856738
## 1FON  -1.6244165 -0.6163498 -1.49970567  0.566496746 -0.13722855
## 1VAU  -3.8392802  0.8580030  1.52406233  0.503972805  0.60386976
## 1DAM   2.8777837 -0.4384994  0.14794681  0.026945728 -0.10629942
## 2BOU   0.6591295 -1.1234093 -0.89904777  0.909888684 -0.29839212
## 1BOI   1.4442031 -1.0612182 -0.68301031  1.204860213 -0.01914242
## 3EL   -0.1886607  0.8581779 -0.85159139 -1.851929127  0.56044692
## DOM1  -0.6582326 -0.4270815  0.48455047  0.248117782  1.69897162
## 1TUR  -1.0690730  0.2301602  1.49245782 -0.194288316 -1.50392162
## 4EL    0.4768726  0.4852073  1.23008094 -0.078196117 -1.20411213
## PER1   1.1591611  0.6625783  1.17334777 -0.298600619 -1.05161409
## 2DAM   1.8503275 -0.7224950  0.13474072 -0.680443110 -0.28833529
## 1POY   1.5443544 -0.4589019  0.02493772 -0.316373161 -0.36560125
## 1ING   0.5498577 -1.0520191 -1.23586229  0.007324811  0.23526535
```

```
## 1BEN  0.1880902 -1.2609589 -0.57777633  1.358947942 -0.36773244
## 2BEA  1.4100775 -1.5077947  1.23996264  0.235908680  1.58499095
## 1ROC -0.8738803 -0.3378355  2.01267085  0.251176289  0.63357323
## 2ING -3.9973507 -0.5605301 -1.17647506  0.799222995 -0.63818454
## T1    1.1623182  3.5408746 -0.32016898  1.079161117  0.02639492
## T2    0.5911084  3.8568076 -1.07104113  0.133183514  0.62066955
```

```
res.pca.w.L1.1$eig
```

```
##          eigenvalue percentage of variance cumulative percentage of variance
## comp 1  2.953254141          33.312935920          33.31294
## comp 2  1.873149351          21.129270057          54.44221
## comp 3  1.082348860          12.208979140          66.65119
## comp 4  0.881901164           9.947913573          76.59910
## comp 5  0.604481735           6.818600886          83.41770
## comp 6  0.392231431           4.424400984          87.84210
## comp 7  0.332176653           3.746978431          91.58908
## comp 8  0.231162135           2.607526828          94.19661
## comp 9  0.161102662           1.817250536          96.01386
## comp 10 0.100884078           1.137980227          97.15184
## comp 11 0.083294954           0.939573542          98.09141
## comp 12 0.070252190           0.792450153          98.88386
## comp 13 0.033660364           0.379691514          99.26355
## comp 14 0.021481970           0.242318287          99.50587
## comp 15 0.019210626           0.216697354          99.72257
## comp 16 0.012241490           0.138084960          99.86065
## comp 17 0.008559353           0.096550162          99.95720
## comp 18 0.001801935           0.020325971          99.97753
## comp 19 0.001585659           0.017886359          99.99541
## comp 20 0.000406479           0.004585115          100.00000
```

Compare with MFA

```
res.mfa.L1.1 <- MFA(wine[,1:20],group = c(2,5,3,10),type = c("n","s","s","s"),graph = F)
res.mfa.L1.1$ind$coord
```

```
##          Dim.1      Dim.2      Dim.3      Dim.4      Dim.5
## 2EL  0.3297217 -0.3578156 -0.47475980  1.772718606  0.20494894
## 1CHA -1.9921118 -0.5669002 -0.67531935  2.132658250 -0.18856738
## 1FON -1.6244165 -0.6163498 -1.49970567 -0.566496746 -0.13722855
## 1VAU -3.8392802  0.8580030  1.52406233 -0.503972805  0.60386976
## 1DAM  2.8777837 -0.4384994  0.14794681 -0.026945728 -0.10629942
## 2BOU  0.6591295 -1.1234093 -0.89904777 -0.909888684 -0.29839212
## 1BOI  1.4442031 -1.0612182 -0.68301031 -1.204860213 -0.01914242
## 3EL  -0.1886607  0.8581779 -0.85159139  1.851929127  0.56044692
## DOM1 -0.6582326 -0.4270815  0.48455047 -0.248117782  1.69897162
## 1TUR -1.0690730  0.2301602  1.49245782  0.194288316 -1.50392162
## 4EL  0.4768726  0.4852073  1.23008094  0.078196117 -1.20411213
## PER1  1.1591611  0.6625783  1.17334777  0.298600619 -1.05161409
## 2DAM  1.8503275 -0.7224950  0.13474072  0.680443110 -0.28833529
## 1POY  1.5443544 -0.4589019  0.02493772  0.316373161 -0.36560125
## 1ING  0.5498577 -1.0520191 -1.23586229 -0.007324811  0.23526535
## 1BEN  0.1880902 -1.2609589 -0.57777633 -1.358947942 -0.36773244
```

```
## 2BEA  1.4100775 -1.5077947  1.23996264 -0.235908680  1.58499095
## 1ROC -0.8738803 -0.3378355  2.01267085 -0.251176289  0.63357323
## 2ING -3.9973507 -0.5605301 -1.17647506 -0.799222995 -0.63818454
## T1   1.1623182  3.5408746 -0.32016898 -1.079161117  0.02639492
## T2   0.5911084  3.8568076 -1.07104113 -0.133183514  0.62066955
```

```
res.mfa.L1.1$eig
```

```
##          eigenvalue percentage of variance cumulative percentage of variance
## comp 1  2.953254141           33.312935920           33.31294
## comp 2  1.873149351           21.129270057           54.44221
## comp 3  1.082348860           12.208979140           66.65119
## comp 4  0.881901164            9.947913573           76.59910
## comp 5  0.604481735            6.818600886           83.41770
## comp 6  0.392231431            4.424400984           87.84210
## comp 7  0.332176653            3.746978431           91.58908
## comp 8  0.231162135            2.607526828           94.19661
## comp 9  0.161102662            1.817250536           96.01386
## comp 10 0.100884078            1.137980227           97.15184
## comp 11 0.083294954            0.939573542           98.09141
## comp 12 0.070252190            0.792450153           98.88386
## comp 13 0.033660364            0.379691514           99.26355
## comp 14 0.021481970            0.242318287           99.50587
## comp 15 0.019210626            0.216697354           99.72257
## comp 16 0.012241490            0.138084960           99.86065
## comp 17 0.008559353            0.096550162           99.95720
## comp 18 0.001801935            0.020325971           99.97753
## comp 19 0.001585659            0.017886359           99.99541
## comp 20 0.000406479            0.004585115           100.00000
```

Now, your turn. Do the same thing for the second node (still, at the first level of the hierarchy, the finest one).

You have just performed two MFAs: one with 4 blocks, one with 2 blocks.

3. MFA at the second (last) level of the hierarchy : my first HMFA

As explained in the lecture, an HMFA is nothing else but a sequence of MFAs: run an MFA (based on PCAs) on the two matrices of coordinates obtained from the MFAs on the first 4 blocks, and on the 2 remaining blocks. Don't forget to build a vector of weights for your PCA. Compare the results with the **HMFA()** function.

Good luck.